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# **Ontogenetic analysis of Anisian (Middle Triassic) ptychitid ammonoids from Nevada, USA**

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**Abstract.**—*Ptychites* is among the most widely distributed ammonoid genera of the Triassic and is namesake of a family and superfamily. However, representatives of the genus mostly show low-level phenotypic disparity. Furthermore, a large number of taxa are based on only a few poorly preserved specimens, creating challenges to determine ptychitid taxonomy. Consequently, a novel approach is needed to improve ptychitid diversity studies. Here, we investigate *Ptychites* spp. from the middle and late Anisian of Nevada. The species recorded include *Ptychites embreei* n. sp., which is distinguished by an average conch diameter that is much smaller and shows a more evolute coiling than most of its relatives. The new species ranges from the *Gymnotoceras mimetus* to the *Gymnotoceras rotelliformis* zones, which makes it the longest-ranging species of the genus. For the first time, the ontogenetic development of *Ptychites* was obtained from cross sections where possible. Cross-sectioning highlights unique ontogenetic trajectories in ptychitids. This demonstrates that, despite showing little phenotypic disparity, *Ptychites* was highly ontogenetically differentiated, and thus the high taxonomic diversity at the species level is justified for the species investigated.

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# Introduction

Ptychitid ammonoids appear at the lower-middle Anisian boundary with Malletoptychites, as well constrained only in the Tethys Himalaya (Krystyn et al., 2004), and are a typical component of the open-marine ammonoid assemblages during Anisian and partially Ladinian times (Balini, 1998). The family fills the gap after a minor ammonoid extinction event when almost all grambergiids disappeared (Konstantinov, 2008). The type genus itself, Ptychites, is one of the most characteristic ammonoids in the fossil record that was erected by Mojsisovics in Neumayr (1875), based on material from the Tethys Realm. Only a limited number of species was known in the early years after erecting the genus, but Mojsisovics' (1882) monograph boosted its importance. This work is regarded as a milestone in the history of Triassic ammonoids and chronostratigraphy (e.g., Tozer, 1971, 1984; Balini et al., 2010; Lucas, 2010; Jenks et al., 2015). Mojsisovics enlarged the number of species of Ptychites, and advanced the organization of this genus in several groups. After the group featured prominently in Mojsisovics (1882), it became one of the guide fossils for Triassic correlations. Its iconic status was also reflected by being a part of Ernst Haeckel's ammonoid selection in his influential book "Kunstformen der Natur"-a trendsetting issue, connecting science and art more

than a century ago (Haeckel, 1899, 1900). In fact, Ptychites has been described from almost all over the world: (1) Nevada (Smith, 1914; Monnet and Bucher, 2005); (2) British Columbia (McLearn, 1948; Tozer, 1994); (3) Spitsbergen (Lindström, 1865; Mojsisovics, 1886; Köhler-Lopez and Lehmann, 1984); (4) the Himalayas (Diener, 1895a, 1907, 1913; Waterhouse, 1994, 1999, 2002a; Krystyn et al., 2004); (5) the Northern Alps (Hallstatt area, Schreyeralm Limestone, condensed Ammonitico-Rosso facies; Mojsisovics, 1882; Diener, 1900); (6) the Balaton Highlands (Vörös, 2018), and (7) the Dinarids and Hellenids (Han Bulog Limestone; von Hauer, 1892; Renz, 1910; Salopek, 1911; Pomoni and Tselepidis, 2013). In the Triassic of Spitsbergen and the Western Tethys, namely the wider Alpine and the Himalayan regions, the genus Ptychites is especially characteristic (e.g., Mojsisovics, 1886; Weitschat and Lehmann, 1983; Harland and Geddes, 1997; Balini, 1998). Therefore, scientists introduced the terms "Ptychitenkalke" (Ptychites limestone; Mojsisovics, 1882, 1886; Gugenberger, 1927; Rosenberg, 1952) and "Ptychites beds" (Spath, 1921; Harland and Geddes, 1997). Ptychites were well adapted to quite a large number of different paleoenvironments (Balini, 1998). Despite this fact, the genus shows a low morphological disparity. The new species described herein does not challenge this picture.

In this paper, we describe a new species of *Ptychites* and discuss the taxonomic diversity and morphologic disparity of this genus during the Middle Triassic of the west coast of North America. Our study area in north-western Nevada,

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USA, belongs to the world's most complete low-paleolatitude sequences, revealing late Anisian ammonoid faunas (Monnet and Bucher, 2005). The continuous sequences, which include a very diverse and abundant ammonoid fauna, provide a good basis for ontogenetic studies on a high-resolution scale. Due to their distinctive ontogenetic trajectories (model curves), ptychitids will act as an important cornerstone in future quantification of ontogenetic analyses.

Because *Ptychites* is found all over the world, this study also contributes to the worldwide correlation of Middle Triassic sediments. Representatives of this group were described from many different localities all over the world. However, most of these records originate from condensed facies, with significant uncertainty regarding the number and age of the faunas, and the composition of the populations. This makes correlative work particularly challenging. The problems of correlation and condensation are discussed by Tozer (1971) and are, for example, reported from Epidauros (Greece) by Krystyn and Mariolakos (1975) and Krystyn (1983). Furthermore, Balini (1998, p. 144) emphasized that the alpha taxonomy of *Ptychites* is characterized by a lack of information on the stratigraphic relationships between the type specimens. The study of ptychitid ammonoids therefore holds great potential for both biostratigraphic and paleobiological work.

# Geological setting and material

The bulk of the fossil material used here was collected by members of the Geosciences Collection of the University of Bremen (Germany). It derives from the Muller and Favret Canyon of the Augusta Mountains (Pershing County), north-western Nevada, USA (see Fig. 1). A complete section of the upper portion of the late Anisian Fossil Hill Member of the Favret Formation and the lowermost part of the early Ladinian Home Station Member of the Augusta Mountain Formation was meticulously documented and measured. Furthermore, J. Jenks collected additional material in Rieber Gulch and Favret Canyon of the Augusta Mountains, Pershing County, and the Wildhorse-McCoy Mine area, Churchill County (see also Fig. 1). Since the fossil material of J. Jenks was loosely collected, no measured sections are associated with this material. However, the sites where the fossil material was found are thoroughly documented and the biostratigraphic framework is well known (Jenks et al., 2015).

Biostratigraphically, *Ptychites* spp. from Nevada that are the focus of this study were collected in the *Balatonites shoshonensis* and the *Gymnotoceras mimetus–Gymnotoceras rotelliformis* zones of the Fossil Hill Member (middle and late Anisian; see Fig. 2). The Fossil Hill Member consists of alternating layers of calcareous siltstone and mudstone with lenticular limestone. The rich fauna of the succession primarily consists of halobiid bivalves and ammonoids. Ceratitids are quite abundant and diverse throughout the member. The Anisian faunas of the Humboldt Range were previously described in the 19<sup>th</sup> and early 20<sup>th</sup> century (Gabb, 1864; Hyatt and Smith, 1905; Smith, 1914). Recently, Silberling and Nichols (1982) and Monnet and Bucher (2005) refined the original alpha taxonomy and the biostratigraphy.

# Methods and conventions

In order to underpin the description of *Ptychites embreei* new species, we performed an ontogenetic analysis of selected specimens of *Ptychites*. The methods introduced by Korn (2010) and Klug et al. (2015) were used. All samples used for ontogenetic analysis were first removed from the rock matrix by mechanical preparation and were then measured along the longest axis. The conch dimensions of the growth stages were obtained from digitized sketches of high-precision cross-sections intersecting the protoconch. In order to find a non-destructive method, a CT scan of selected specimens with a GE Phoenix v device, tome, x s 240 with a nanoray tube NF 180 kV was performed at the University of Erlangen, Germany. Unfortunately, the differences in density were marginal, and therefore the contrast of the internal structures on the scan images were not sufficient for further analysis.

The basic conch parameters (dm: diameter; ww: whorl width; wh: whorl height) for all available specimens were measured at every distinct growth stage (i.e., half whorl), starting at the protoconch. For the ontogenetic analysis, the growth parameters whorl expansion rate (WER<sub>n</sub> =  $[dm_n/dm_{n-0.5}]^2$ ), whorl width index (WWI<sub>n</sub> = ww<sub>n</sub>/wh<sub>n</sub>), umbilical width index (UWI<sub>n</sub> = uw<sub>n</sub>/dm<sub>n</sub>), and the conch width index (CWI<sub>n</sub> = ww<sub>n</sub>/dm<sub>n</sub>) were calculated (for further explanations see Korn, 2010; Klug et al., 2015).

Ontogenetic morphospace.—The growth parameters WER, UWI, and CWI were also analyzed in a principal component analysis (PCA). The dataset comprises the values for all distinct growth stages of an individual. In contrast to most other ontogenetic studies using ternary plots or multivariate statistics (e.g., Korn and Klug, 2007; Klug et al., 2016; Walton and Korn, 2017, 2018), herein every individual is defined by the sum of all parameters of all ontogenetic stages. In order to omit missing values in the analysis, the PCA data set was limited to the last growth stage of the specimen with the fewest number of half whorls (here growth stage number 5.0; see Appendix). All parameters are numbered consecutively, starting with the first half whorl (i.e., WER<sub>0.5</sub>, CWI<sub>0.5</sub>, UWI<sub>1.0</sub>) to the last one of the analysis (i.e., WER<sub>5.0</sub>, CWI<sub>5.0</sub>, UWI<sub>5.0</sub>). Therefore, the space opened up by this analysis is not a classical morphospace showing the morphology of an individual at a specific growth stage, but in an artificial state of combined morphologies of different ontogenetic stages. It illustrates how the ontogeny of the groups differ. To prevent confusion, we introduce the term "ontogenetic morphospace." The PCA with correlation matrix was run using PAST (version 3.25; Hammer et al., 2001).

*Suture lines.*—The preservation of the ammonoids occasionally permits the drawing of suture lines. Among the fossil material herein, GSUB C13194 (*P. guloensis* Tozer, 1994) and C13196 (*P. gradinarui* Bucher, 1992) were the only specimens with a nicely preserved suture line. We used the suture terminology of Wedekind (1916), as applied by Kullmann and Wiedmann (1970) and modified by Korn et al. (2003)—E: external lobe; A: adventive lobe (that corresponds

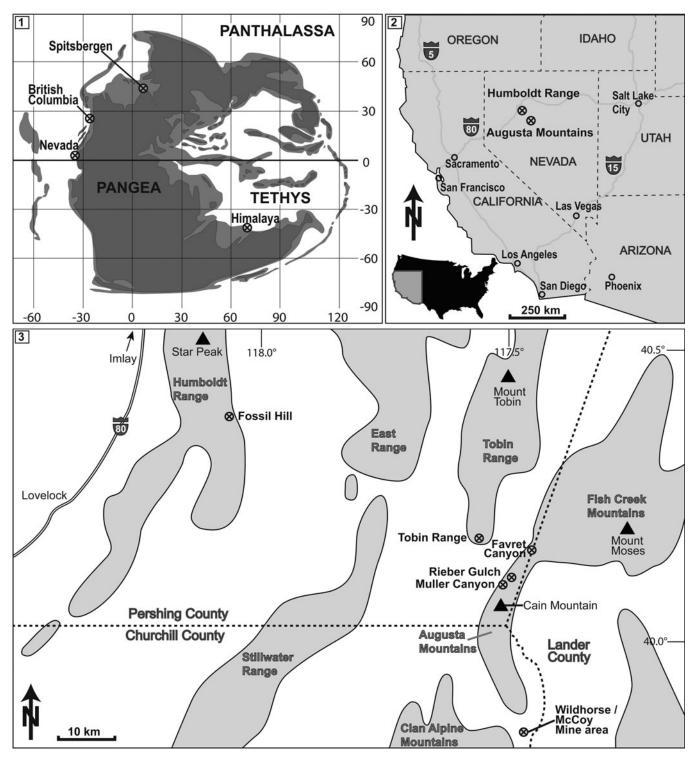


Figure 1. (1) Middle Triassic paleogeographical setting. Nevada as well as other important localities of Ptychites spp. are marked. Redrawn from Péron et al. (2005), Brayard et al. (2006), and Skrzycki et al. (2018). (2, 3) Location of the study area in NW Nevada, USA. The most important localities of Fossil Hill Member outcrops are marked.

to letter L of the traditional nomenclature); U: umbilical lobe; I: internal lobe; E/A (that is E/L of traditional nomenclature) is the saddle between E and A; A/U (that is L/U of traditional nomenclature) corresponds to the saddle between A and U.

Repositories and institutional abbreviations.—Geosciences Collection of the University of Bremen (GSUB), Germany; Paleontological Institute and Museum University of Zurich (PIMUZ), Switzerland; New Mexico Museum of Natural History & Science (NMMNH), Albuquerque, New Mexico,

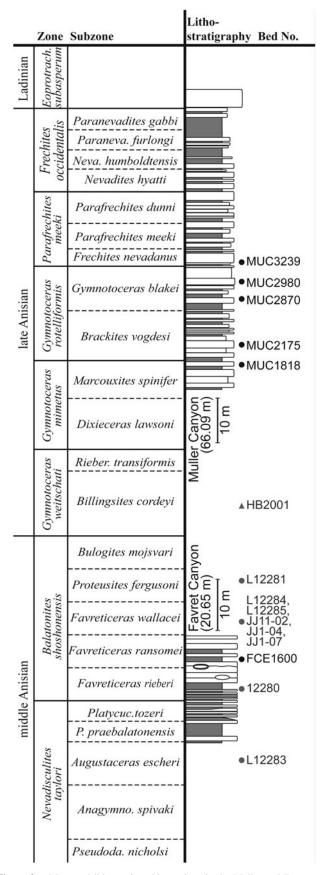


Figure 2. Measured lithostratigraphic sections in the Muller and Favret canyons of the Augusta Mountains, Pershing County, NW Nevada, USA from where our specimens were collected. Black dots: Beds within our measured sections; Gray dots: JJ-localities documented by J. Jenks, Salt Lake City, Utah, USA; Gray triangle: HB-locality, documented by H. Bucher, Zurich, Switzerland (Monnet and Bucher, 2005).

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USA. The abbreviation JJ refers to localities of J. Jenks, Salt Lake City, Utah, USA, and HB refers to localities of H. Bucher, Zurich, Switzerland.

In the synonymy list we used '[n.s.]' for publications we have not seen, because we could not get hold of a copy of that paper.

# Systematic paleontology

Order Ceratitida Hyatt, 1884 Superfamily Ptychitoidea Mojsisovics, 1882 Family Ptychitidae Mojsisovics, 1882 Genus *Ptychites* Mojsisovics in Neumayr, 1875

*Type species.*—*Ammonites rugifer* Oppel, 1863 (designated by Tozer, 1994, see discussion on p. 133). Tozer (1981, p. 94) was used as reference for the family-group taxonomy.

Ptychites guloensis Tozer, 1994 Figures 3.5–3.7, 4

1994 *Ptychites guloensis*; Tozer, p. 133, pl. 48, figs. 1, 2, textfigs. 35d, e.

*Holotype.*—Holotype is GSC 70993 from the Sulphur Mountain Formation, Minor Zone, near south end of Hook Lake, NTS Kinuseo Falls (GSC loc. 83873), Canada; several paratypes from other localities in the same area.

*Diagnosis.*—The diagnosis of *Ptychites guloensis* by Tozer (1994, p. 133) is as follows: "*Ptychites* attaining a diameter of at least 70 mm; H about 50 per cent, W 60–70 per cent, U about 15 per cent of diameter. Whorl section ovoid, the flanks and venter merging to form a perfect arch. Distinct ribbing absent, growth striae nearly or perfectly radial. Suture line with four lateral saddles, the outer two large and the inner two small. The inner two are depressed in relation to the large saddles weakly bifid. Moderately sized to large *Ptychites* with a perfectly rounded venter. Rather narrow umbilicus with a steep umbilical wall. Almost smooth conch with only fine growth striae."

*Occurrence.*—Favret Canyon, Augusta Mountains, Pershing County: GSUB loc. FCE, *F. ransomei* Subzone, *B. shoshonensis* Zone, Fossil Hill Member of the Augusta Mountain Formation. According to Tozer (1994, p. 133), *P. guloensis* also occurs in the Middle Anisian, Middle Triassic, *H. minor* Zone, Toad Formation of north-eastern British Columbia.

*Description.*—Measurements of the selected specimen are provided in Table 1. Specimen GSUB C13194 (Fig. 3.5-3.7) is a complete conch with a maximum diameter of 26.71 mm. The pachyconic conch (ww/dm = 0.69) is subinvolute (uw/dm = 0.22) and has a perfectly rounded venter. The narrow umbilicus is deeply incised revealing a steep umbilical wall. The umbilical shoulders merge into the venter in a wide arch. The largest part of the shell is not preserved. The remnants of the shell and some

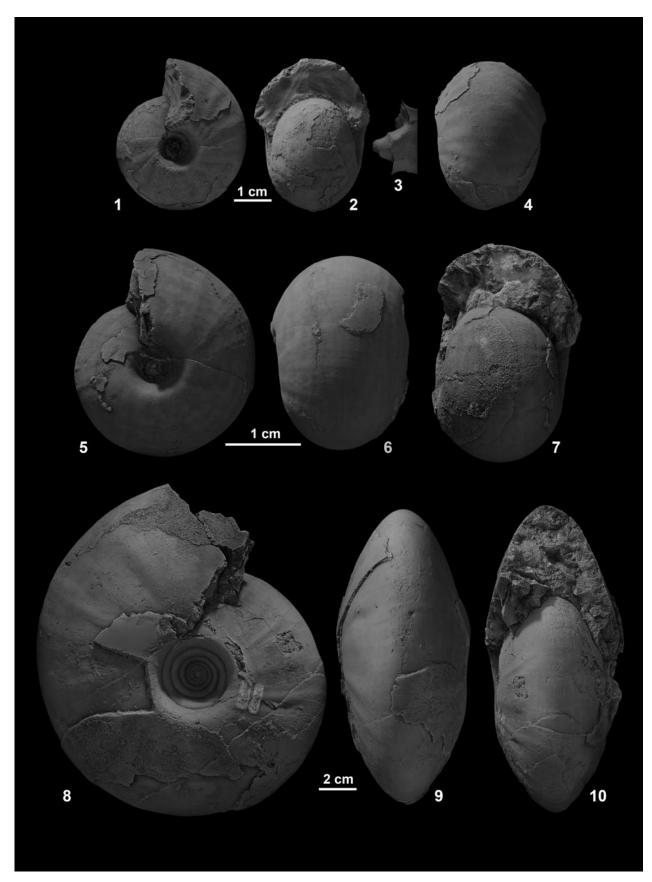


Figure 3. (1–4) *Ptychites wrighti*, from north side of Favret Canyon, Augusta Mountains, Pershing County; (3) cast of deeply incised and funnel-shaped umbilicus, NMMNH 80882. (5–7) *Ptychites guloensis*, Favret Canyon, Augusta Mountains, Pershing County, GSUB C13194. (8–10) *Ptychites gradinarui*, Favret Canyon, Augusta Mountains, Pershing County, GSUB C13194. (8–10) *Ptychites gradinarui*, Favret Canyon, Augusta Mountains, Pershing County, GSUB C13194. (8–10) *Ptychites gradinarui*, Favret Canyon, Augusta Mountains, Pershing County, GSUB C13194. (8–10) *Ptychites gradinarui*, Favret Canyon, Augusta Mountains, Pershing County, GSUB C13194. (8–10) *Ptychites gradinarui*, Favret Canyon, Augusta Mountains, Pershing County, GSUB C13194. (8–10) *Ptychites gradinarui*, Favret Canyon, Augusta Mountains, Pershing County, GSUB C13194. (8–10) *Ptychites gradinarui*, Favret Canyon, Augusta Mountains, Pershing County, GSUB C13196.

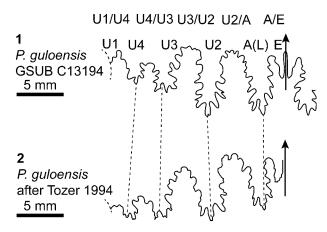


Figure 4. Suture line of *Ptychites guloensis*, (1) GSUB C13194 compared to (2) Tozer (1994, p. 444, fig. 35e). Bracketed letters indicate traditional suture nomenclature.

imprints on the steinkern however reveal that the shell was smooth, bearing some fine growth striae.

The major elements of the suture line of specimen GSUB C13194 (Fig. 4.1) are uniformly large, namely with an U3/U2, U2, A/U2, and an A that are of a similar extent. The A lobe is bifid, with the endings slightly less incised compared to the other major sutural elements. The U2/A tapers towards the aperture. The E/A is slender and less strongly denticulate. The U1/U4 shows a prominent, slender spur. The suture line of GSUB C13194 shows only minor differences to the sutures redrawn from Tozer (1994) (Fig. 4.2). The latter differs by a trifid A lobe that is slightly smaller, a U2/A that is not tapering, and the U1/U4 that lacks a spur.

# Materials.—One specimen (GSUB C13196).

*Remarks.*—Köhler-Lopez and Lehmann (1984) illustrated the ontogenetic development of the suture line of *Aristoptychites*, and thus demonstrated that the traditional nomenclature should be modified in Ptychitidae. In this respect, Tozer (1994, p. 133) refers to "four lateral saddles," these are the U2/A, U3/U2, U4/U3, and U1/U4 of the ontogenetic nomenclature used herein. The diagnosis of the suture line of *P. guloensis* given by Tozer (1994, p. 133) is as follows: "[...] with four lateral saddles, the outer two large and the inner two small. The inner two are depressed in relation to the large saddles. The outer large saddles are not bifid; the inner small saddles weakly bifid." However, this does not characterize the species because the features can be found in other species of *Ptychites* as well. Nevertheless, the Canadian specimen shows typical features of *Ptychites*, such as the rather broad and rounded outline of the

**Table 1.** Measurements in mm of one specimen of *Ptychites guloensis* Tozer, 1994 collected in the Fossil Hill Member of the Favret Formation at the Muller Canyon locality in the Augusta Mountains, Pershing County, Nevada, USA. For further details on the bed number, see Figure 2 ("Bed No."). uw: maximum umbilical width; ww: maximum whorl width; dm: maximum diameter of shell.

Locality	Specimen	uw	ww	dm	uw/dm	ww/dm
FCE1600	GSUB C13194	5.82	18.33	26.71	0.22	0.69

U3/U2 and U2/A and the multi point indentations of the lobes. Although we consider the preservation of GSUB C13194 as good, we cannot rule out that the slightly more slender and irregular indentations of the U3/U2 and U2/A and the different shape of the lowermost tip of the A lobe with fairly broad and simple indentations are a matter of preservation.

### Ptychites wrighti McLearn, 1946 Figure 3.1–3.4

- 1946 Ptychites wrighti; McLearn, p. 3, pl. 4, fig. 5 [n. s.].
- 1948 Ptychites wrighti; McLearn, p. 12, pl. 4, fig. 5.
- 1969 Ptychites wrighti; McLearn, p. 56, text-fig. 31, pl. 10, fig. 1a-c.
- 1994 Ptychites wrighti; Tozer, p. 134, pl. 48, figs. 3, 4.

*Holotype.*—According to McLearn (1969), the holotype (GSC 6442) is from the Toad Formation, far up "McTaggart Creek," west slope of Mount Wooliever, Sikanni Chief River valley (GSC loc. 10731), Canada.

*Diagnosis.*—Small to moderately sized species of *Ptychites* with a rounded to subtriangular venter and a rather narrow umbilicus with an abrupt umbilical shoulder. The conch bears very weak folds and ribs.

*Occurrence.*—North side of Favret Canyon, Augusta Mountains, Pershing County: NMMNH loc. L 12283, *A. escheri* Subzone, *N. taylori* Zone. According to Tozer (1994), *P. wrighti* also occurs in the middle Anisian, Middle Triassic, *H. minor* Zone?, Toad Formation of north-eastern British Columbia.

*Description.*—Measurements of the selected specimen are provided in Table 2. Specimen NMMNH 80882 (Fig. 3.1–3.4) is a complete conch with a maximum diameter of 38.74 mm. The pachyconic shell (ww/dm = 0.74) is subinvolute (uw/dm = 0.26) revealing a deeply incised umbilicus (Fig. 3.3) and an abrupt umbilical shoulder. Rounded to subtriangular shoulder. The flanks are covered with very weak, irregular and slightly rursiradiate ribs and folds. The length of the body chamber exceeds one whorl.

Materials.—One specimen (NMMNH 80882).

*Remarks.*—The diagnosis for this species is newly established here, due to a lack of a former diagnosis. The occurrence of this species seems to be restricted to the open water fauna of the Panthalassic Ocean. The available material does not allow an ontogenetic analysis. The suture line published in McLearn (1969) shows that the sutural elements of this species are

**Table 2.** Measurements in mm of one specimen of *Ptychites wrighti* McLearn, 1946 collected by J. Jenks in the Fossil Hill Member of the Favret Formation, Pershing County, Nevada, USA. For further details on the bed number, see Figure 2 ("Bed No."). uw: maximum umbilical width; ww: maximum whorl width; dm: maximum diameter of shell.

Locality	Specimen	uw	WW	dm	uw/dm	ww/dm
L 12283	NMMNH 80882	10.18	28.75	38.74	0.26	0.74

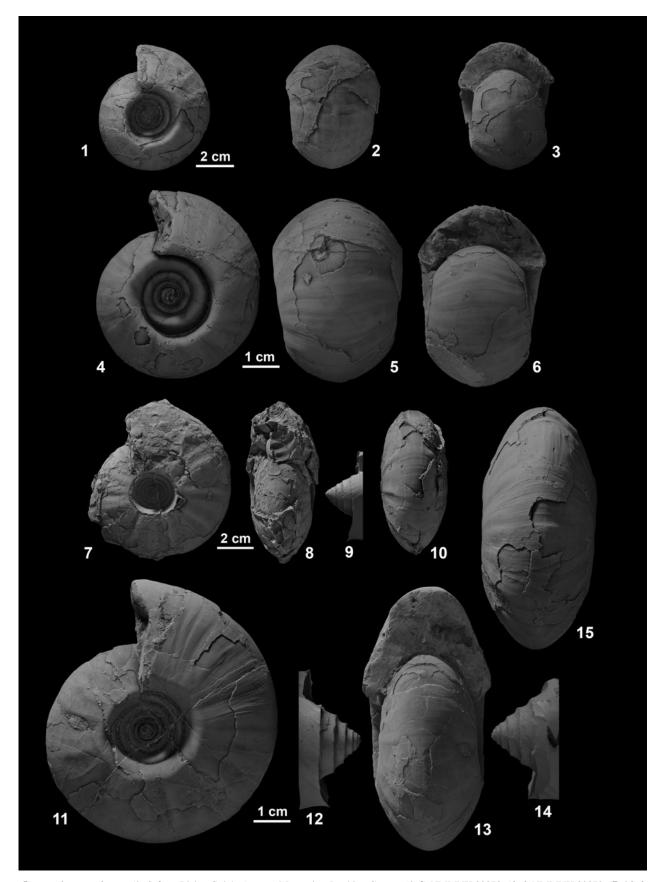


Figure 5. Ptychites gradinarui (1–6) from Rieber Gulch, Augusta Mountains, Pershing County, (1–3) NMMNH 80878, (4–6) NMMNH 80879; (7–14) from the Wildhorse-McCoy mine area, Churchill County, (7–10) GSUB C11443, (9) cast of deeply incised and funnel-shaped umbilicus; (11–14) NMMNH 80880, (12, 14) casts of deeply incised and funnel-shaped umbilicus.

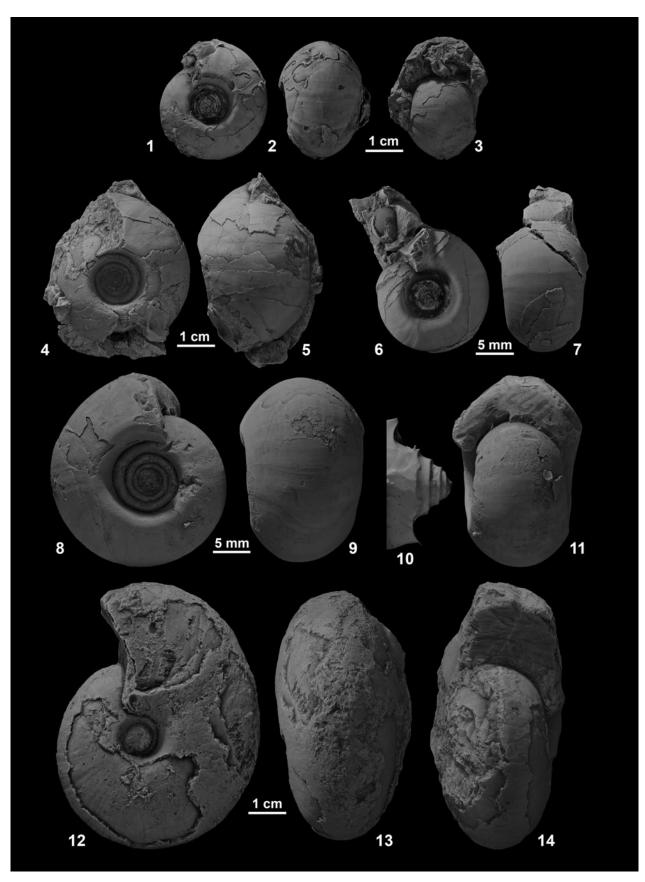


Figure 6. (1–11) *Ptychites gradinarui* (1–5) from Rieber Gulch, Augusta Mountains, Pershing County, (1–3) GSUB C11442, (4, 5) GSUB C11441; (6–11) from the Wildhorse-McCoy Mine area, Churchill County, (6, 7) GSUB C11440, (8–11) NMMNH 80877, (10) cast of deeply incised and funnel-shaped umbilicus. (12–14) *Ptychites densistriatus* from the south side of Favret Canyon, Augusta Mountain, Pershing County, NMMNH 80881.

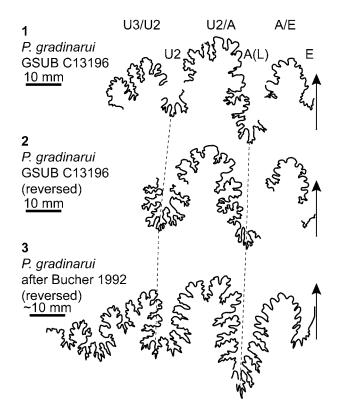


Figure 7. Adult suture of *Ptychites gradinarui*. Bracketed letters indicate traditional suture nomenclature. (1, 2) Suture lines drawn from specimen GSUB C13196, of which (2) is reversed. (3) Reversed suture line redrawn from Bucher, 1992, text-figure 22a.

comparatively strongly denticulate with deep incisions and a rather weak frilling.

*Ptychites gradinarui* Bucher, 1992 Figures 3.8–3.10, 5, 6.1–6.11, 7, 8

- 1968 Ptychites cf. P. domatus (Hauer); Silberling and Tozer, p. 37.
- 1992 *Ptychites gradinarui*; Bucher, p. 439, pl. 9, figs. 11, 12, pl. 10, figs. 1–4, pl. 11, figs. 21–26, text-fig. 22.
- 2007 Ptychites gradinarui; Jenks et al., p. 36, pl. 18, figs. a, b.

*Holotype.*—The holotype USNM 448264, the paratypes USNM 448262, USNM 448265–448267, and the plesiotype USNM 448263 are all stored in the collection of the National Museum of Natural History in Washington D.C, USA (Bucher, 1992).

*Diagnosis.*—Rather large species of *Ptychites* reaching a diameter of 90 mm and in rare cases more than 250 mm (see Bucher, 1992, p. 440). The conch of juvenile specimens is mostly pachyconic. The later ontogenetic stages, however, show two different morphotypes: pachyconic-subevolute (ww/dm ~0.70; uw/dm ~0.40) and discoidal-subinvolute (ww/dm ~0.50; uw/dm ~0.30). Furthermore, the conch bears a smooth ornament of irregular, rectiradiate to slightly falcoid ribs and growth striae. The internal mold of juvenile specimens shows growth constriction.

*Occurrence.*—Wildhorse-McCoy Mine area, Churchill County: NMMNH locs. L 12281 (*P. fergusoni* Subzone), 12285 and J. Jenks loc. JJ1-04, JJ1-07 (*F. wallacei* Subzone) of the *B. shoshonensis* Zone. Rieber Gulch, Augusta Mountains, Pershing County: NMMNH loc. L 12284 and JJ11-02, *F. wallacei* Subzone, *B. shoshonensis* Zone. Favret Canyon, Augusta Mountains, Pershing County: GSUB loc. FCE1600, *F. ransomei* Subzone, *B. shoshonensis* Zone.

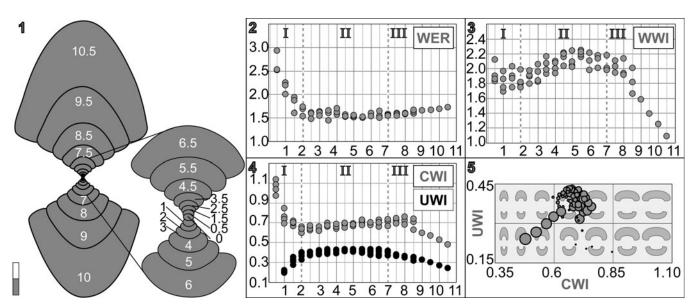
*Description.*—Measurements of the selected specimens are provided in Table 3. The largest pachyconic (ww/dm = 0.76) and robust specimen (NMMNH 80879; Fig. 5.4–5.6) has a diameter of dm = 66.66 mm. The subevolute to evolute umbilicus (uw/dm = 0.44) is very deeply incised with a steep umbilical wall and a very abrupt umbilical shoulder. The venter is subtriangular. The ornamentation of the conch consists of smooth and irregular, rectiradiate to slightly falcoid ribs, and very fine growth striae. The partly preserved shell of the largest specimen (GSUB C13196; Fig. 3.8–3.10) is very thick (1.5 mm at the venter and >3 mm along the umbilical shoulder).

The partially preserved suture line of GSUB C13196 is illustrated in Figure 7. The umbilical part of the line is missing. The widths of U3/U2, U2, A/U2, A, and A/E of the herein described specimen (Fig. 7.1, 7.2) are comparable to those of the specimen published in Bucher, 1992 (Fig. 7.3 herein). The A lobe is trifid. As with the E/A illustrated in Bucher, 1992, this saddle is slender and less strongly denticulate than the others are. Bucher (1992) did not illustrate the conch of the specimen he analyzed. However, since the whorl height of the specimen indicated is ~80 mm, the specimen must have had a similar conch size to the specimen of this study (whorl height of specimen GSUB C13196: 88.30 mm).

The largest discoidal (ww/dm = 0.46) specimen used for the ontogenetic analysis (GSUB C11443; Fig. 5.7–5.10), has a diameter of dm = 85.62 mm. The subinvolute umbilicus (uw/ dm = 0.27) is also very deeply incised (Fig. 5.9). The umbilical wall is a little bit less steep than that of their more robust conspecifics. The venter of the discoidal specimen is subtriangular. The ornamentation, however, equals the robust specimens.

*Ontogenetic description.*—The ontogenetic development of *P. gradinarui* is illustrated in Figure 8, and the raw data of the analysis are supplied in the Appendix. The whorl expansion rate (WER; Fig. 8.2) shows a triphasic behavior with a strong decrease in the earliest stages and a rather stable intermediate phase. In phase III, the WER increases again, indicating an acceleration of growth.

The values for the whorl width index (WWI) are more scattered than the other series (Fig. 8.3). Nevertheless, a triphasic development of the growth trajectories can be observed. In phase I and II, the conch width index (CWI) and the umbilical width index (UWI) describe opposing parabolas (Fig. 8.4). *Ptychites gradinarui* shows a trend of developing a slightly more pachyconic and less evolute conch in their early stages, resulting in a clock-wise progression (Fig. 8.5). In contrast to UWI, the CWI is a triphasic trajectory. Therefore, at growth stage 8.0, the two indices decouple. Whereas the UWI sticks to the parabolic curve progression, CWI quite abruptly decreases after



**Figure 8.** Ontogenetic analysis of *Ptychites gradinarui*. (1) Cross section of the largest discoidal specimen GSUB C11443, scale bar units 5 mm. (2–4) Ontogenetic development of the whorl expansion rate (WER<sub>n</sub> =  $(dm_n/dm_{n-0.5})^2$ ), whorl width index (WWI<sub>n</sub> =  $ww_n/wh_n$ ), umbilical width index (UWI<sub>n</sub> =  $ww_n/dm_n$ ), and the conch width index (CWI<sub>n</sub> =  $ww_n/dm_n$ ) plotted against number of half whorls (ontogenetic stages). (5) Ratio between UWI and CWI of the available specimens. Bubble size refers to number of half whorl; the picture in the background shows the shape of the last complete whorl (developed by Korn, 2010). Roman numbers refer to interpretation of different life phases; I: Hatchling, II: Juvenile; III: Subadult–adult; for more detailed explanations see Walton and Korn (2017, p. 713).

whorl 8.0, causing a distinct buckle in the growth trajectories (Fig. 8.5). This means that in later ontogenetic stages, the species develops more discoidal and less evolute conches. Following the notation of Walton and Korn (2017), the morphologic development of *P. gradinarui* is characterized by a C-mode ontogeny.

In general, all the trajectories shown in Figure 8.2–8.5 show a change in direction towards the end of the phase II (growth stage 5.0 to 8.0; roughly corresponds to growth size of 9–27 mm; see also Appendix). These changes in the progression of the trajectories are interpreted to mark the transition from juvenile to adult stages. The analysis of a large pachyconic specimen would allow testing whether the two morphotypes (discoidal and pachyconic, see above) could be explained by sexual dimorphism. If more globous variants of this species show the same ontogenetic trends, at around the same growth stage, this would underpin the hypothesis of sexual dimorphism. However, no appropriate specimen was available.

Table 3. Measurements in mm of selected specimens of *Ptychites gradinarui* Bucher, 1992 collected by J. Jenks and us in the Fossil Hill Member of the Favret Formation, Churchill and Pershing counties, Nevada, USA. For further details on the bed number, see Figure 2 ("Bed No."). uw: maximum umbilical width; ww: maximum whorl width; dm: maximum diameter of shell; (): Fragmented specimens, estimated values; \*: specimen used for ontogenetic analysis, cast present.

Locality	Specimen	uw	WW	dm	uw/dm	ww/dm
L 12284	NMMNH 80878	(21.09)	36.75	52.48	0.40	0.70
L 12284	NMMNH 80879	29.32	50.46	66.66	0.44	0.76
L 12284	NMMNH 80880	25.83	34.95	69.62	0.37	0.50
JJ11-02	GSUB C11441*	13.07	28.55	(38.27)	0.34	0.75
JJ11-02	GSUB C11442*	10.31	23.67	32.48	0.32	0.73
JJ1-04	GSUB C11440*	6.00	11.15	15.49	0.39	0.72
JJ11-07	GSUB C11443*	22.98	39.81	85.62	0.27	0.46
L12281	NMMNH 80877	10.39	17.53	25.90	0.40	0.68
FCE1600	GSUB C13196	43.49	79.00	177.00	0.25	0.45
-						

*Materials.*—Nine specimens (NMMNH 80877–80880, GSUB C11440–C11443, GSUB C13196).

*Remarks.*—The diagnosis for this species is newly established here, due to a lack of a former diagnosis. This species appears to be endemic to Nevada, with its closest ally, *P. sahadeva* Diener, 1895a, from the Himalayan region according to Bucher (1992). Among the material herein, two different morphotypes can be distinguished—a more depressed type with a subtriangular venter and a slightly narrower umbilicus, and a robust variant with very abrupt umbilical shoulders. However, the ornamentation with irregular fine ribs, growth striae, and weak depressions are very similar. Furthermore, smaller specimens herein and the specimens illustrated in Bucher (1992) seem to be intermediate to these two morphotypes. Because the biostratigraphic and geographic ranges of both morphotypes are also overlapping, the two morphotypes were assigned to one species, dimorphism cannot be excluded.

#### Ptychites densistriatus Bucher, 1992 Figures 6.12–6.14, 9.1–9.3

1992 Ptychites densistriatus; Bucher, p. 441, pl. 9, figs. 1–10.

*Holotype.*—According to Bucher (1992), the holotype (USNM 448261), the paratypes (USNM 448259, 448260), and the plesiotype (USNM 448258) are all stored in the collection of the National Museum of Natural History in Washington D.C., USA.

*Diagnosis.*—Moderately sized species of *Ptychites* with a subinvolute (uw/dm  $\sim$ 0.25) and discoidal to pachyconic conch

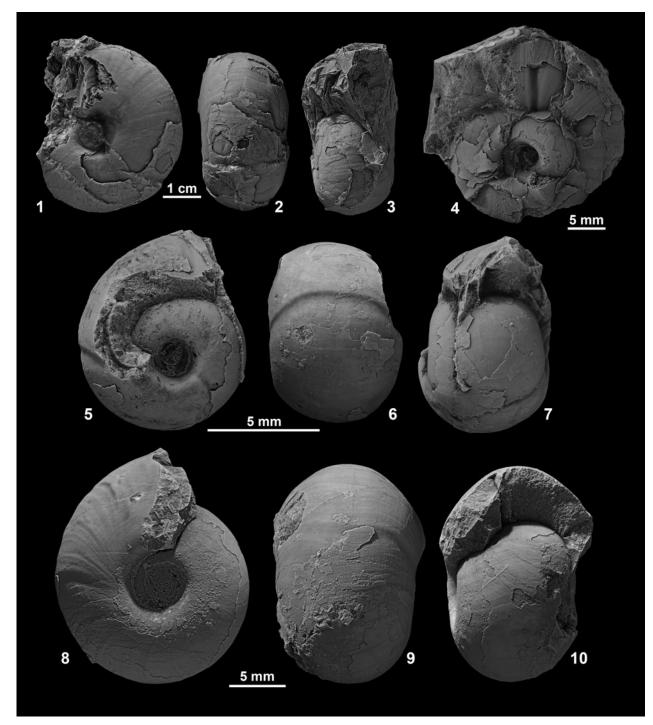


Figure 9. (1–3) Ptychites densistriatus from Favret Canyon, Pershing County, Nevada, GSUB C11439. (4–10) Ptychites embreei n. sp. from Muller Canyon, Augusta Mountains, Pershing County, (4) GSUB C8273 (paratype), (5–7) GSUB C8254, (8–10) GSUB C8287 (paratype).

(ww/dm ~0.60). Whereas juvenile specimens are clearly pachyconic, the conch gets more depressed towards later ontogenetic stages. More rounded umbilical shoulder. Smooth shell with an ornament of thick radial growth striae.

Occurrence.—Favret Canyon, Augusta Mountains, Pershing County: NMMNH loc. L 12280, *F. rieberi* Subzone, *B. shoshonensis* Zone. *Description.*—Measurements of the selected specimens are provided in Table 4. Specimen NMMNH 80881 (Fig. 6.12–6.14) is a complete conch with a maximum diameter of 53.49 mm. The discoidal to pachyconic shell (ww/dm = 0.60) is subinvolute (uw/dm = 0.24), revealing a deeply incised umbilicus with a steep umbilical wall and a narrowly rounded umbilical shoulder. The specimen is slightly ovoid. Furthermore, the almost smooth surface of the conch only bears smooth growth striae.

*Materials.*—Two specimens (NMMNH 80881, GSUB C11439).

*Remarks.*—The diagnosis for this species is newly established here, due to a lack of a former diagnosis. To our knowledge, this species in endemic to Nevada. Preservation of the available material did not allow a sutural and ontogenetic analysis.

# Ptychites embreei new species Figures 9.4–9.10, 10–13

2005 *Ptychites* sp. indet; Monnet and Bucher, p. 49, pl. 23, fig. 9.

*Holotype.*—GSUB C9453 (Fig. 12), Fossil Hill Member of the Favret Formation, Muller Canyon in the Augusta Mountains, Pershing County, Nevada, USA.

*Paratypes.*—Five specimens GSUB C8273 (Fig. 9.4), C8287 (Fig. 9.8–9.10), C8289 (Fig. 10.7–10.9), C8280 (Fig. 11.1–11.3), and C9458 (Fig. 11.7–11.9), Fossil Hill Member of the Favret Formation, Muller Canyon in the Augusta Mountains, Pershing County, Nevada, USA.

*Diagnosis.*—Very small to small-sized and depressed *Ptychites* attaining a diameter <30 mm at maximum. Conch subinvolute to subevolute (uw/dm ~0.29) and pachyconic (ww/dm ~0.73). Smooth surface of shell with a fine ornament of striae. More rounded umbilical shoulder.

Occurrence.—Muller Canyon, Augusta Mountains, Pershing County: GSUB loc. MUC, from *M. spinifer* Subzone, *G. mimetus* Zone to *P. meeki* Subzone, *P. meeki* Zone. McCoy Mine, Churchill County: Loc. HB 2001, *B. cordeyi* Subzone, *G. weitschati* Zone (Monnet and Bucher, 2005, specimen PIMUZ 25361).

*Description.*—Measurements of the selected specimens are provided in Table 5. The holotype (GSUB C9453; Fig. 12) is a complete specimen with a maximum diameter of 29.77 mm. Because of its large size, compared to other representatives of this new species, it is interpreted as an adult specimen; there are no other criteria for maturity. The pachyconic (ww/dm = 0.61) shell is subevolute (uw/dm = 0.37) and reveals a deeply incised umbilicus with a steep umbilical wall and a distinctive umbilical shoulder. The surface of the shell is smooth and bears a very fine ornament of striae. The venter is perfectly rounded and smooth.

**Table 4.** Measurements in mm of selected specimens of *Ptychites densistriatus* Bucher, 1992 collected by J. Jenks in the Fossil Hill Member of the Favret Formation. Pershing County, Nevada, USA. For further details on the bed number, see Figure 2 ("Bed No."). uw: maximum umbilical width; ww: maximum whorl width; dm: maximum diameter of shell; (): fragmented specimen, estimated value;\*\*: specimen used for ontogenetic analysis, preservation not sufficient, cast present.

Locality	Specimen	uw	WW	dm	uw/dm	ww/dm
L 12280	NMMNH 80881	12.76	32.02	53.49	0.24	0.60
L 12280	GSUB C11439**	11.26	25.33	(43.03)	0.26	0.59

In general, smaller specimens are subinvolute and slightly more depressed than larger specimens (see Table 5). Furthermore, the umbilical shoulder is more abrupt. The internal molds of some specimens show growth constrictions (C8273, Fig. 9.4; C8254, Fig. 9.5, 9.6; C8287, Fig. 9.9).

Ontogenetic description.—The ontogenetic development of P. embreei n. sp. is illustrated in Figure 13, and the raw data of the analysis are supplied in the Appendix. The whorl expansion rate (WER; Fig. 13.2) shows a regular behavior with a strong decrease in the earliest stages, followed by more stable state towards the end of phase II. The slightly higher values of half whorl 7.5 and 8.5 suggest a possible acceleration of growth in later ontogenetic stages.

The values for the whorl width index (WWI; Fig. 13.3) are more scattered than the other series. However, considering the shape of the CWI trajectory (Fig. 13.4) and the more regular WWI of *P. gradinarui* (Fig. 8.3), it can be assumed that the progression of WWI is at least triphasic.

During phase I and II, the trajectories for the conch width index (CWI) and the umbilical width index (UWI) are inverse (Fig. 13.4), indicating a close relationship between these two indices. The development of UWI and CWI is similar to the C-mode ontogeny introduced by Walton and Korn (2017). However, towards later ontogenetic stages, the UWI and CWI are decoupled, which distinguishes P. embreei n. sp. from regular C-mode ontogeny. Whereas the conches of early stage P. embreei n. sp. are more globous and more involute, in the course of their growth they build slightly more discoidal and more evolute conches, resulting in a counterclockwise progression (Fig. 13.5). The decoupling of the CWI and UWI results in a distinct buckle in the progression. In general, all the trajectories (Fig. 13.2–13.5) that are long enough show a change towards the end of the second phase (growth stage 5.0 to 8.0; roughly corresponds to a growth size of 12-19 mm). These changes in the progression of the trajectories most probably mark the transition from the juvenile to the adult stage.

*Etymology.*—The species was named in honor of geologist Patrick G. Embree (Orangevale, CA, USA) for his contributions and broad support of the research on the Triassic of Nevada.

*Materials.*—In total, we collected 38 specimens of *P. embreei* n. sp. in Muller Canyon of the Augusta Mountains, Pershing County, NW Nevada, USA. Two specimens: GSUB C9642, C9643, from bed No. MUC1818; 10 specimens: GSUB C9453, C9455–C9462, C8564, from bed No. MUC2175; one specimen: GSUB C8423, from bed No. MUC2870; 19 specimens: GSUB C8254, C8265, C8267, C8269, C8270, C8272–C8280, C8285–C8287, C8290, from bed No. MUC2980; and six specimens: GSUB C9619, C9621–C9624, C10313; from bed No. MUC3239. The specimen PIMUZ 25361 was illustrated in Monnet and Bucher (2005) and is stored in the original collection of the Paleontological Institute and Museum University of Zurich, Switzerland. For further explanation on the beds see Figure 2.

*Remarks.*—Specimen PIMUZ 25361, referred to as *Ptychites* sp. indet. by Monnet and Bucher (2005), is regarded as

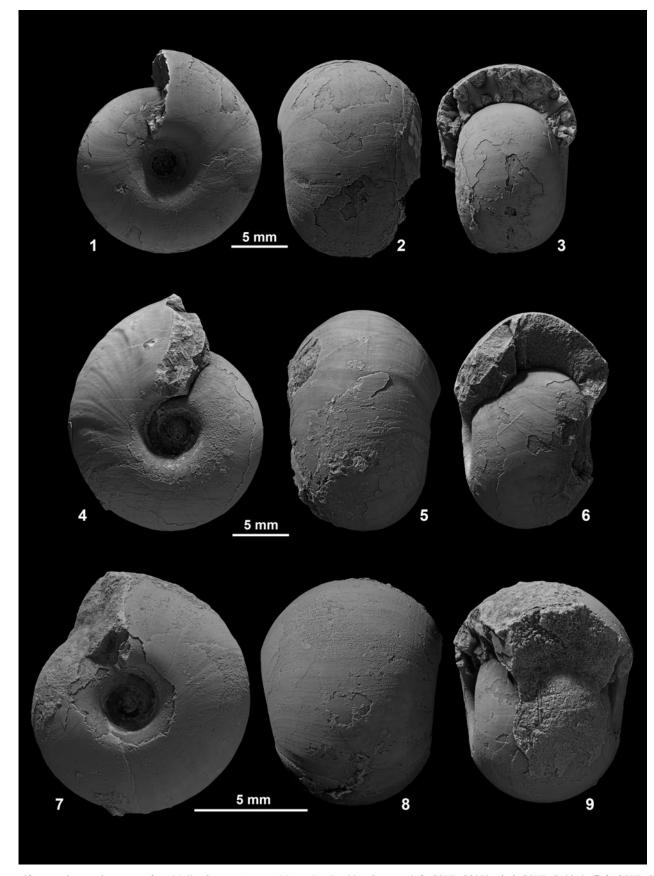


Figure 10. Ptychites embreei n. sp. from Muller Canyon, Augusta Mountains, Pershing County. (1–3) GSUB C8272, (4–6) GSUB C10313, (7–9) GSUB C8289 (paratype).

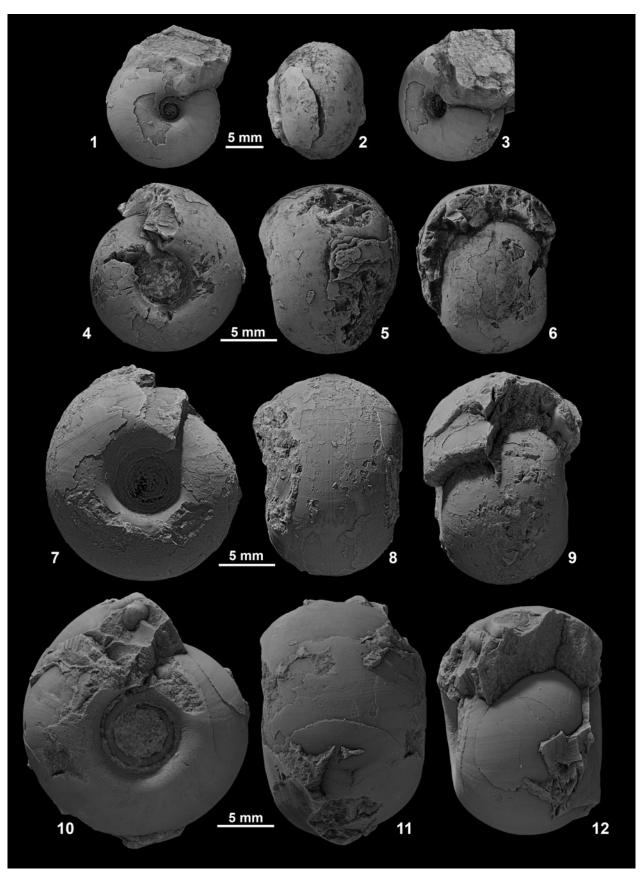


Figure 11. *Ptychites embreei* n. sp. from Muller Canyon, Augusta Mountains, Pershing County. (1–3) GSUB C8280 (paratype), (4–6) GSUB C9458 (paratype), (7–9) GSUB C9455, (10–12) GSUB C9642.

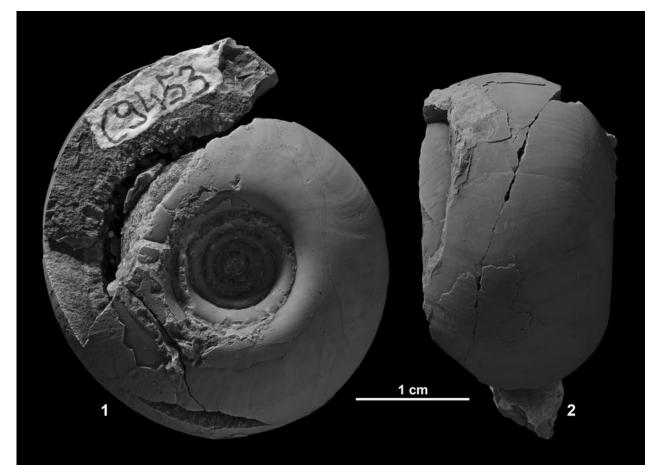
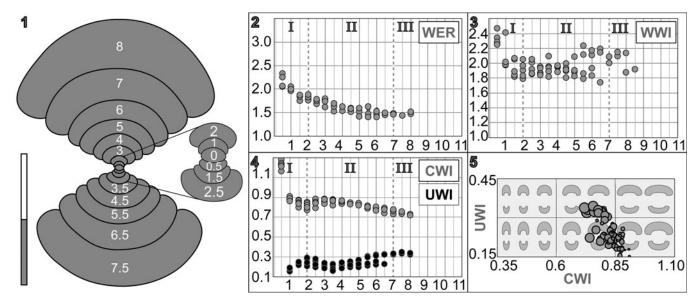


Figure 12. (1, 2) Holotype GSUB C9453 of Ptychites embreei n. sp. from Muller Canyon, Augusta Mountains, Pershing County.



**Figure 13.** Ontogenetic analysis of *Ptychites embreei* n. sp. (1) Cross section of specimen GSUB C9642, scale bar units 5 mm. (2–4): Ontogenetic development of the whorl expansion rate  $(WER_n = (dm_n/dm_{n-0.5})^2)$ , whorl width index  $(WWI_n = ww_n/wh_n)$ , umbilical width index  $(UWI_n = uw_n/dm_n)$  and the conch width index  $(CWI_n = ww_n/dm_n)$  plotted against number of half whorls (ontogenetic stages). (5) Ratio between UWI and CWI of the available specimens. Bubble size refers to number of half whorl; the picture in the background shows the shape of the last complete whorl (developed by Korn, 2010). Roman numbers refer to interpretation of different life phases; I: Hatchling, II: Juvenile; III: Subadult–adult; for more detailed explanations see Walton and Korn (2017).

Table 5. Measurements in mm of selected specimen of *Ptychites embreei* n. sp. collected in the Fossil Hill Member of the Favret Formation at the Muller Canyon locality in the Augusta Mountains. Pershing County. Nevada. USA. Further details on the bed number see Figure 2 ("Bed No."). uw: maximum umbilical width; ww: Maximum whorl width; dm: maximum diameter of shell; (): fragmented specimen, estimated value; \*: specimens used for ontogenetic analysis, cast present; \*\*: specimen used for ontogenetic analysis, preservation not sufficient, cast present; H: holotype.

Depth	Specimen	uw	ww	dm	uw/dm	ww/dm
MUC3239	GSUB C10313**	4.84	13.28	18.66	0.26	0.71
MUC2980	GSUB C8287	1.95	8.24	10.95	0.18	0.75
MUC2980	GSUB C8280	3.69	11.80	16.24	0.23	0.73
MUC2980	GSUB C8272*	4.31	13.22	17.74	0.24	0.75
MUC2980	GSUB C8289	2.56	8.10	10.25	0.25	0.79
MUC2980	GSUB C8254	1.8	6.06	7.97	0.23	0.76
MUC2980	GSUB C8276*	1.47	6.20	7.55	0.19	0.82
MUC2870	GSUB C8423*	3.43	8.60	11.29	0.30	0.76
MUC2175	GSUB C9453 H	11.02	18.20	(29.77)	0.37	0.61
MUC2175	GSUB C9455*	5.82	13.63	19.07	0.31	0.71
MUC2175	GSUB C9458	4.53	11.45	14.65	0.31	0.78
MUC1818	GSUB C9642*	6.99	14.76	20.53	0.34	0.72
HB 2001	PIMUZ 25361	2.0	7.1	10.5	0.19	0.68

conspecific with *P. embreei* n. sp. Among the ptychitids of Nevada, *P. embreei* n. sp. covers by far the largest time span. It remains to be clarified whether this is due to biological processes or reflects a bias caused by more intensive sampling associated with this study relative to prior work.

There are two more globular genera occurring in sediments of the same age in Nevada: *Humboldtites* Silberling and Nichols, 1982 and *Proarcestes* Mojsisovics, 1893. Both genera differ from representatives of *P. embreei* n. sp. through their very involute to closed umbilicus and the more compressed shape. Furthermore, their suture lines have much narrower main saddles and a more constricted base.

Mojsisovics (1882, p. 244) divided all species of *Ptychites* in five different groups: P. rugiferi, P. megalodisci, P. subflexuosi, P. opulenti, and P. flexuosi. *Ptychites embreei* n. sp. is included into the group of P. opulenti because it agrees in being predominantly globular. The distinguishing morphologic features of different species of this group are given in Table 6. In summary, representatives of *P. embreei* n sp. differ from other *Ptychites* species mainly in having smaller growth size, the absence of ribs, and the more rounded umbilical shoulder.

The range of intraspecific variability among the material described herein is rather small. The largest differences seem to result from ontogenetic processes, which is also the case with certain Paleozoic ammonoids (e.g., Korn, 2017; Korn et al., 2018), in which the trajectories for CWI and UWI are inverses (Fig. 13.4), indicating a close relationship between these two indices. This means that, in agreement with Buckman's first Rule of Covariation (Westermann, 1966), compression co-occurs with less evolute conches.

#### Morphospace

In order to analyze the ontogenetic morphospaces of *Ptychites gradinarui* and *P. embreei* n. sp., a principal component analysis was performed (Fig. 14). Despite the low number of available specimens, the ontogenetic morphospaces of the two species are clearly separated in the PCA plot. The first two principal components of the PCA explain ~81.52% (PC 1: 73.76%; PC

Downloaded From: https://bioone.org/journals/Journal-of-Paleontology on 25 Apr 2024 Terms of Use: https://bioone.org/terms-of-use 2: 7.76%) of the observed variation. The raw data for the analysis are provided in the Appendix.

The first principal component (PC1) is mainly dominated by values of the umbilical width index (UWI) and the conch width index (CWI), which have similar loadings. On principal component 2 (PC2), however, values for the whorl expansion rate (WER) alone feature dominantly. Therefore, the axes of the analysis reflect the following: (1) high PC 1 values express a more depressed and lower values a more compressed conch shape, and (2) high PC 2 values mainly coincide with a higher WER. The right part of the morphospace is thus occupied by more pachyconic, and the left part with rather discoidal conches. Most of the ontogenetic changes are captured within changes of the umbilical diameter and the conch width. Even though *P. gradinarui* generally reaches a much larger growth size, the whorl expansion rate seems to be of minor importance for the distinction of the ontogenetic pathways of these species.

#### Geographic and stratigraphic occurrence of ptychitids

During the Middle Triassic, representatives of *Ptychites* were widely distributed in the Panthalassic as well as the Tethys Ocean. Here we present a summary of the biostratigraphic distribution of *Ptychites* spp. in the most significant domains (Fig. 15). The different biostratigraphic occurrences of *P. guloensis* in Nevada and British Columbia are possibly biased by a low number of specimens. However, it is apparent that the faunas of Nevada and British Columbia are similar in composition to a certain degree.

Representatives of Flexoptychites, closely allied to Ptvchites, were also described from the isolated Germanic Muschelkalk Sea (e.g., Claus, 1921, 1955; Urlichs and Kurzweil, 1977), which is characterized by an endemic ammonoid fauna. In fact, ptychitids are known from the Lower and the Upper Muschelkalk, probably reflecting that the endemism is higher in the Upper Muschelkalk (see Urlichs and Mundlos, 1985; Kaim and Niedźwiedzki, 1999). However, based on the description and illustrations in the former, it cannot be verified with certainty whether the described specimens really belong to Ptychites or closely allied forms. Furthermore, Urlichs and Mundlos (1985) and Balini (1998) doubted that those occurrences were part of a living population and suggested a postmortem drift of the shells from the Tethys. For those reasons, the Germanic Muschelkalk Basin was not considered in the summary of the biostratigraphical occurrences of ptychitids during the Anisian stage (Fig. 15).

# Discussion

Representatives of *Ptychites* can be found in sediments that were deposited in the Panthalassic (e.g., Smith, 1914; McLearn, 1948; Tozer, 1994; Monnet and Bucher, 2005) and Tethyan Oceans (e.g., Diener, 1913; Waterhouse, 1994, 1999, 2002a, b). Due to its almost global distribution, the genus *Ptychites* has been broadly discussed in the literature, but limited research has been done in recent years. Especially the correlation between the Tethyan and Panthalassic faunas still demands further attention. In the Panthalassic realm, the co-occurrence of ptychitds in

Table 6. Morphologic comparison of different species of *Ptychites* of the *P. opulentus* group to the newly introduced species *P. embreei* n. sp. For biostratigraphic and geographic distribution, see Figure 15. U and uw: maximum umbilical width; D and dm: maximum diameter of conch; S.s.: Small specimens; L.s.: Large specimens.

<ul> <li>11, 12, pl. 10, figs. 1–4, pl. 11 figs. 21–26)</li> <li><i>P. wrighti</i> McLearn, 1946 (p. 3 pl. 4, fig. 5)</li> <li><i>P. guloensis</i> Tozer, 1994 (p. 133, 444, figs. 35d, e, pl. 58, figs. 1, 2)</li> <li><i>P. densistriatus</i> Bucher, 1992 (p. 440, pl. 9, figs. 1–10)</li> <li><i>P. trochleaeformis</i> (Lindström, 1865, p. 3, pl. 1, fig. 2)</li> <li><i>P. hamatus</i> Tozer, 1994 (p. 134 pl. 65, figs. 13, 14, pl. 67, fis 1–4 pl. 71, fig. 2a, b, text-figs 48d, 50a, 54b)</li> </ul>	Average conch	Venter and conch		Umbilic			Ontogenetic
Species	size	outline	Sculpture	Width	Shape	Adult suture line	development
<i>Ptychites embreei</i> n. sp.	Small, < 30 mm	Venter perfectly rounded Depressed	Smooth surface, no ribs, fine growth striae S.s. some growth constrictions	S.s. subinvolute: uw/dm < 0.30 L.s. subevolute: uw/ dm > 0.30	Distinct, but slightly rounded umbilical shoulder	Unknown	Ontogenetic pathways see Fig. 8
(p. 439, text-fig. 22, pl. 9, figs. 11, 12, pl. 10, figs. 1–4, pl. 11,	Larger	Subtriangular venter L.s. more compressed	L.s. fine ribbing Regular shallow growth constrictions	S.s. more evolute	Umbilical shoulder angular	Four lateral saddles, U2/A largest and highest, A/E high and slender compared to broad U3/U2, A/E lower than U2/A, usually weakly bifid. A lobe deepest lobe. Indentations with irregular fringes.	For comparison of ontogenetic pathway see Figs. 5 and 8, respectively
<i>P. wrighti</i> McLearn, 1946 (p. 3, pl. 4, fig. 5)	Larger	Slightly angular venter More compressed	Slight ribbing	More involute: U/D of holotype is 0.20 (McLearn, 1948)	Umbilical shoulder angular	Unknown	
(p. 133, 444, figs. 35d, e, pl.	Much larger	Similar	Very fine but regular ribbing	More involute	Similar	Four lateral saddles, U2/A most prominent, only slightly larger and higher than U3/U2. A/E high and slender compared to U3/U2. U4/U3 and U1/U4 distinctly smaller than outer saddles, low number of simple indentations. U2 lobe is deepest. Even indentations only, there are no fringes.	
	Larger	Much higher whorl section More compressed and ovoid conch	Similar	S.s. more evolute L.s.more involute	Umbilical shoulder even more rounded	Unknown	
	Much larger (108 mm; Lindström, 1865)	L.s. more compressed	Regular ribbing	More involute: U/D = 20/108 = 0.19 (Lindström, 1865)	Umbilical shoulder angular	Unknown	
<i>P. hamatus</i> Tozer, 1994 (p. 134, pl. 65, figs. 13, 14, pl. 67, fis. 1–4 pl. 71, fig. 2a, b, text-figs. 48d, 50a, 54b)		L.s. more compressed	Similar	More involute	Umbilical wall less steep Umbilical shoulder more angular	Five lateral saddles, U2/A highest. U2/A, U3/2, U4/U3 almost same breadth, saddles fairly gently reducing in height from U2/A towards umbilical seam. A lobe much deeper than others. Mainly low indentations and only few fringes.	to more compressed
<i>P. progressus</i> Mojsisovics, 1882 (p. 259, pl. 67, figs. 4, 6)	Larger	More compressed	Regular growth constrictions	Much more involute S.s. uw/dm = 6/38 = 15.8; L.s. uw/dm = 10/67 = 14.9; Mojsisovics, 1882: p. 260	"Stairlike" (terraced) surface of umbilical wall (Mojsisovics, 1882)	Four lateral saddles. U2/A highest, U2/A, U3/2 and U4/U3 almost same breadth, saddles only gently reducing in size from U2/A towards umbilical seam. Center of U4/U3 deeply incised, almost half the height of the saddle. A lobe deepest, but U2 lobes only very slightly shallower. A number of regular fringes.	Transition from more involute to more evolute

	Average conch	Average conch Venter and conch		Umbilic			Ontogenetic
Species	size		Sculpture	Width	Shape	Adult suture line	development
P. cuminghami Diener, 1913 (p.70, pl. 10, fig. 4)	Much larger (188 mm; Diener, 1913)	Much more compressed	Smooth ribbing	Much more involute	Umbilical wall less steep	Five lateral saddles, U2/A most prominent one, clearly larger than all others. A/E higher and larger compared to U3/U2, with mostly low and indistinct indentations distinguished from other ptychitid sutures discussed. U4/U3 and U1/U4 distinctly lower than outer saddles and U1/U4 with low number of simple indentations only. A lobe clearly deepest and most prominent. Suture line generally irregular, with irregular and	
						regular fringes, low and rounded indentations (?preservational artifact).	
P. opulentus Mojsisovics, 1882 (p. 259, pl. 73, figs. 1–4)	Larger	S.s. conch is wider than high L.s. more compressed	S.s. regular growth constrictions Smooth ribbing	S.s. much narrower (uw/ Similar dm = 13/105 = 12.4; Mojsisovics, 1882)	Similar	Five lateral saddles, U2/A most prominent, much larger than others with narrow base compared to 048. AE Bigher and larger compared to U3/ U2, big main indentations. U4/U3 and U1/U4 distinctly smaller than outer saddles, low number of simple indentations. Stutue line with low number of irregular fringes. A lobe is clearly the deepest and most prominent lobe.	Transition from way more depressed to more compressed

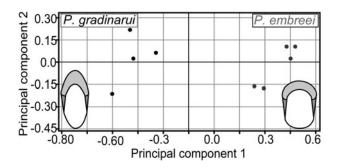


Figure 14. Principal Component Analysis (PCA) of combined ontogenetic stages of all available specimens of *Ptychites gradinarui* and *Ptychites embreei* n. sp. The parameters whorl expansion rate (WER), umbilical width index (UWI), and conch width index (CWI) were used. Every individual is defined by the sum of all parameters of all ontogenetic stages. Black dots *P. gradinarui*, gray dots *P. embreei* n. sp.

Nevada and British Columbia supports the statement of Ji and Bucher (2018) that low- and mid-paleolatitude regions were well connected during the Middle Triassic. This stresses the importance of re-evaluation of the alpha taxonomy of ptychitid species by novel or underexplored methods, as performed in this study.

*Ontogenetic analysis.*—Ammonoid generic diversity reached its maximum during the Triassic Period (Brayard et al., 2009). At present, few studies have investigated trends in morphological disparity of Triassic ammonoids (Monnet et al., 2015). McGowan (2004, 2005) and Brosse et al. (2013) carried out important foundational research in this field. Although the background data of both studies differ significantly, both come to the same conclusion: the taxonomic diversity and morphologic disparity of Triassic ammonoids are decoupled. However, it is open to debate whether the high diversity is also biased by taxonomic over-splitting (Forey et al., 2004; De Baets et al., 2013) of the ammonoid faunas.

A method, whose potential is far from being fully exploited, is the analysis of ontogenetic trajectories obtained from longitudinal cross-sections. The accretionary growth of ammonoids with conservation of juvenile stages allows the investigation of complete ontogenetic transformations of a set of traits, such as the conch geometry and septal characters (Korn, 2012). Therefore, ontogenetic analyses are an ideal tool to unravel phylogenetic and taxonomic relationships between ammonoid groups (Rieber, 1962). This makes them ideal for the study of evolutionary change in ontogeny through time (Naglik et al., 2015).

Walton and Korn (2017) carried out an extensive comparative ontogenetic analysis of ammonoids within the pachyconic to globular morphospace. They introduced the term C-mode ontogeny, which is by far the most common ontogeny of pachyconic to globular ammonoids. Whereas the herein discussed species *P. gradinarui* shows a C-mode ontogeny, *P. embreei* n. sp. has a different development. In phase I and II, *P. embreei* n. sp. and *P. gradinarui* have opposing trends in their relationships of the CWI and UWI (Figs. 8.5, 13.5). However, both trajectories show a distinct buckle in the curve that marks the decoupling of the UWI and CWI, which is approximately located at an UWI of 0.35 and CWI of 0.70. The change in the direction of the progression marks the onset of the third phase, during which both

Table 6. Continued.

	Zone	Subzone	Bios	tratigraphic distril	bution of <i>Ptychite</i> s	s spp.
	(Nevada, USA)	(Nevada, USA)	<b>Nevada, USA</b> Smith, 1914 Silberling & Nichols,1982 Bucher, 1992 Own data	British Columbia Tozer, 1994	<b>Spitsbergen</b> Weitschat & Lehmann, 1983	<b>Tethyan realm</b> Mojsisovics, 1882 Diener, 1913 Waterhouse, 2002a
"early" Ladinian	Eoprotrachyceras subasperum			P. hamatus		
late Anisian	Frechites occidentalis Parafrechites meeki Gymnotoceras rotelliformis Gymnotoceras mimetus Gymnotoceras weitschati	P. gabbi P. furlongi N. humboldt. P. dunni P. meeki F. nevadanus G. blakei B. vogdesi M. spinifer D. lawsoni R. transiformis B. cordeyi	P. embreei P. embreei P. embreei P. embreei P. embreei	P. hamatus P. trochleaeformis P. trochleaeformis	P. trochleaeformis	P. opulentus P. progressus P. cunninghami
middle Anisian	Balatonites shoshonensis Nevadisculites taylori	B. mojsvari P. fergusoni F. wallacei F. ransomei F. rieberi P. tozeri P. praebalat. P. escheri P. spivaki P. nicholsi	P. gradinarui P. gradinarui P. guloensis P. densistriatus P. wrighti	P. guloensis P. wrighti		

**Figure 15.** Biostratigraphic distribution of Ptychites spp. The biostratigraphic framework and correlation of Nevada, British Columbia, and the Tethyan realm follows Jenks et al. (2015). For the correlation of Spitsbergen, Harland and Geddes (1997) and Weitschat and Lehmann (1983) were used. Only representatives of Ptychites discussed in this publication are listed in this table. Therefore, empty boxes do not necessarily indicate the absence of all Ptychites spp. \* Indicates location of the "Ptychiten Kalke—Ptychites layers" (e.g., Mojsisovics, 1886; Spath, 1921; Gugenberger, 1927; Rosenberg, 1952; Harland and Geddes, 1997). Paleogeographic locations of the localities are provided in Figure 1. \*\* According to Weitschat (1986, p. 253), the preservation of middle Anisian ammonoids of Spitsbergen is not sufficient for a successful zonation of the area. Crosses mark gaps in the ammonoid biostratigraphic framework.

trajectories behave more or less collinear. According to Walton and Korn (2017), the change in conch morphologies during ontogeny could be caused by the adaptation to different niche types in the different life phases. It is questionable, whether the disparity of these two groups is significant enough to suggest two different modes of life during the earliest life phases. Nevertheless, it is very interesting to note that ptychitids have very distinct ontogenetic developments even at the species level.

In general, there is limited literature on ontogenetic analysis of individual species. However, in their study of heteromorph ammonites of the Early Cretaceous, Hoffmann et al. (2019) used similar multivariate methods as described in this study. Their study proved that the statistical evaluation of ontogenetic trajectories of ammonoids provides useful information about diversity and disparity at species level. Our study verifies that the statistical evaluation of ontogenetic processes is applicable to normally coiled planispiral ammonoid species from the Middle Triassic. Important ontogenetic changes can be visualized using univariate (Figs. 8, 13) and multivariate (Fig. 14) methods. Despite a low number of available specimens, the principal component analysis succeeded in separating the two ontogenetic morphospaces of the two ammonoid groups. This highlights the uniqueness of the ontogenetic trajectories and morphospaces that representatives of this group occupy.

Sutures.—The tapering U2/A saddle and the U1/U4 with a slender spur appear to be unique sutural features among ptychitids. However, due to the lack of specimens for comparison, it remains unclear if this is significant. No further features of the suture line of GSUB C13194, *P. guloensis*, seem to be unique (e.g., bifid endings in the A lobe occur in our material as well as in other specimens referred to the genus; sutures of *P. opulentus* Mojsisovics, 1882 [Qingge et al., 1980]; *Flexoptychites* cf. cochleatus [Oppel, 1863] and *P. cf. asura* Diener, 1895b [Win, 1991]). Our examination of published suture lines in ptychitids underlines the opinion of Köhler-Lopez and Lehmann (1984, p. 63) that suture lines of ptychitids vary significantly, "much in degree of incision," but

"not in the number of elements." These authors state that the lateral saddle of the very well-investigated species Aristoptychites kolymensis Kiparisova, 1937 is always extremely small and narrow. This is true for many specimens of closely related genera and their species as well, but there are exceptions to this rule and thus this cannot be generalized for this group (e.g., P. cf. cochleatus in Win, 1991). We see no clear relation of sutural features to the conch morphology of ptychitid genera. The suture lines are highly dependent on the growth stage. The very large specimen GSUB C13196 (P. gradinarui, Figs. 3.8-3.10, 8) shows clearly more incisions of lobes and saddles than specimens in earlier stages. Specimen GSUB C13194 (P. guloensis, Figs. 3.5-3.7, 4) does not show the sutural development and thus we cannot discuss the ontogeny of the suture line of the species based on our material. Nevertheless, the high number of sutural elements at the umbilical seam might indicate a multiplication of elements of the U3 as recorded by Kullmann and Wiedmann (1970). The latter was called a sutural lobe due to its position at the umbilical seam (Wedekind, 1916; "sutural" means umbilical seam in this respect); this term is problematic, though, because it only refers to the position on the shell. Köhler-Lopez and Lehmann (1984) nicely show that the U1 (with multiple subdivisions) can be located at this position as well. Therefore, we agree with Köhler-Lopez and Lehmann (1984) that a U3 developed as a sutural lobe does not characterize Ptychitidae. In fact, the sutures of many species of Ptychites and closely allied genera do not show this feature, including P. compressus Yabe and Shimizu, 1927; P. guloensis; P. opulentus; P. wrighti; Discoptychites megalodiscus (Beyrich, 1967); Flexoptychites flexuosus (Mojsisovics, 1882); and Malletoptychites malletianus (see Diener, 1895a; Onuki and Bando, 1959; McLearn, 1969; Qingge et al., 1980).

# Conclusions

Here we enhance the taxonomic understanding of ptychitids, including a description of *Ptychites embreei* n. sp. from the late Anisian of Nevada. According to the state of the art, this species is the longest-ranging within the group. Furthermore, it fills a gap in the otherwise intensively studied ammonoid fauna of north-western Nevada, USA.

After the Permian/Triassic boundary, Ptychitoidea, Megaphyllitoidea, and Arcestoidea filled the cadicone morphospace (Brosse et al., 2013; De Baets et al., 2016, fig. 7). Despite the wide geographic distribution of ptychitids, they exhibit a remarkably low level of morphological variation within their morphospace. Since all ptychitids have an almost smooth shell, with a subordinate ornamentation only, one of the most important morphological descriptive features of ammonoids (Klug et al., 2015) is not applicable to the group. This means there are narrow limits regarding the shell variability in the cadicone morphospace in the Anisian, with mostly leiostracan forms (smooth shelled ammonoids; Westermann, 1996). However, some features characterizing the species seem to be hidden in a distinct ontogeny (Figs. 8, 13, 14). We emphasize the ontogenetic differences of ptychitids to other Middle Triassic ammonoids of Nevada. Ptychitids, despite their similar morphologies, have unique ontogenetic trajectories, as demonstrated above (Figs. 8, 13). Ontogenetic analyses are therefore an ideal tool to improve the alpha taxonomy of ptychitids.

Since the evaluation of ontogenetic trajectories is a rather descriptive and therefore, to some extent, subjective process, a great potential of this method lies within their statistical quantification and interpretation. This study includes one of the first attempts to quantify the ontogenetic development of individuals using statistical methods. The analysis of the very distinct ontogenetic pathways of ptychitids will serve as an important cornerstone in future studies on the statistical quantification of ontogenetic analyses of ammonoids.

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# Appendix

Morphometric data for the available specimens that were measured on the cross-sections and used for the ontogenetic analysis

GSUB	No. of whorl /								
Specimen	growth	dm	WW	wh	uw				
No.	stage	[mm]	[mm]	[mm]	[mm]	CWI	UWI	WWI	WER
C11442	8.5	32.44	22.99	12.64	10.31	0.71	0.32	1.82	1.64
	8	25.35	18.35	9.49	8.73	0.72	0.34	1.93	1.60
	7.5	20.03	14.49	7.13	7.23	0.72	0.36	2.03	1.58
	7	15.92	11.35	5.66	5.83	0.71	0.37	2.01	1.56
	6.5	12.74	8.90	4.43	4.81	0.70	0.38	2.01	1.64
	6	9.94	6.92	3.49	3.96	0.70	0.40	1.98	1.61
	5.5	7.84	5.58	2.48	3.27	0.71	0.42	2.25	1.50
	5	6.39	4.37	2.09	2.70	0.68	0.42	2.10	1.54
	4.5	5.15	3.55	1.60	2.21	0.69	0.43	2.21	1.52
	4	4.18	2.67	1.34	1.74	0.64	0.42	2.00	1.63
	3.5	3.28	2.20	1.11	1.37	0.67	0.42	1.99	1.66
	3	2.54	1.58	0.81	1.04	0.62	0.41	1.96	1.61
	2.5	2.00	1.24	0.69	0.73	0.62	0.37	1.80	1.59
	2	1.59	1.01	0.58	0.51	0.64	0.32	1.75	1.74
	1.5	1.21	0.87	0.50	0.33	0.72	0.27	1.75	1.87
	1	0.88	0.75	0.38	0.17	0.85	0.19	1.97	2.00
	0.5	0.62	0.71	0.33		1.14		2.12	2.52
	0	0.39	0.64	0.39					
C11441	8.5	37.10	27.47	13.69	12.98	0.74	0.35	2.01	1.59
	8	29.41	22.31	10.43	10.70	0.76	0.36	2.14	1.58
	7.5	23.43	17.45	8.29	8.91	0.74	0.38	2.11	1.60
	7	18.51	13.59	6.23	7.37	0.73	0.40	2.18	1.58
	6.5	14.72	10.70	4.91	6.06	0.73	0.41	2.18	1.55
	6	11.82	8.29	3.75	5.01	0.70	0.42	2.21	1.53
	5.5	9.55	6.71	3.06	4.11	0.70	0.43	2.19	1.52
	5	7.75	5.35	2.38	3.26	0.69	0.42	2.25	1.52
	4.5	6.29	4.28	2.10	2.59	0.68	0.41	2.03	1.57
	4	5.02	3.32	1.60	2.08	0.66	0.41	2.08	1.57
	3.5	4.01	2.79	1.35	1.60	0.70	0.40	2.07	1.60
	3	3.17	1.95	1.06	1.26	0.62	0.40	1.84	1.63
	2.5	2.48	1.62	0.85	0.99	0.65	0.40	1.91	1.61
	2	1.95	1.16	0.64	0.78	0.60	0.40	1.82	1.69
	1.5	1.50	1.00	0.53	0.53	0.66	0.35	1.87	1.94

Continued.

Continued.		

GSUB Specimen	No. of whorl / growth	dm	ww	wh	uw				_	GSUB Specimen	No. of whorl / growth	dm	ww	wh	uw				
No.	stage	[mm]	[mm]	[mm]	[mm]	CWI	UWI	WWI	WER	No.	stage	[mm]	[mm]	[mm]		CWI	UWI	WWI	WER
	1	1.08	0.82	0.44	0.23	0.76	0.21	1.86	2.25		2.5	2.03	1.79	0.87	0.52	0.88	0.26	2.05	1.70
	0.5 0	0.72 0.42	0.78 0.75	0.41 0.42		1.08		1.90	2.93		2 1.5	1.56 1.17	1.31 1.02	0.64 0.49	0.43 0.27	0.84 0.87	0.28 0.23	2.05 2.07	1.78 1.75
C11443	10.5	84.99	40.76	37.38	20.43		0.24	1.09	1.72		1	0.89	0.80	0.41		0.91	0.18	1.97	1.96
	10 9.5	64.76 49.78	33.99 28.30	27.17 20.30	17.28 14.88	0.52 0.57	0.27 0.30	1.25 1.39	1.69 1.66		0.5 0	0.63 0.41	0.79 0.64	0.32 0.41		1.24		2.47	2.32
	9	38.59	23.10	14.60	12.61	0.60	0.33	1.58	1.66	C9642	8	20.50	14.73	7.68	6.94		0.34	1.92	1.52
	8.5		18.91		10.36	0.63	0.35	1.66	1.67		7.5	16.65	12.58	5.88	5.75		0.35	2.14	1.43
	8 7.5	23.20 18.37	15.81 12.69	8.24 6.51	8.45 6.90	0.68 0.69	0.36 0.38	1.92 1.95	1.60 1.55		7 6.5	13.91 11.51	10.80 8.96	5.02 4.30	4.60 3.67	$0.78 \\ 0.78$	0.33 0.32	2.15 2.09	1.46 1.49
	7	14.75	9.83	4.96	6.14	0.67	0.42	1.98	1.55		6	9.44	7.60	3.55	2.93	0.81	0.31	2.14	1.40
	6.5 6	11.86 9.67	7.82 6.55	3.66 3.11	5.10 4.20	0.66 0.68	0.43 0.43	2.14 2.11	1.50 1.54		5.5 5	7.98 6.75	6.42 5.69	2.96 2.69	2.33 1.80	$\begin{array}{c} 0.80\\ 0.84 \end{array}$	0.29 0.27	2.17 2.11	1.40 1.41
	5.5	7.80	5.27	2.37	3.36	0.68	0.43	2.23	1.53		4.5	5.68	4.71	2.26	1.43	0.83	0.25	2.08	1.51
	5 4.5	6.31 5.06	4.21 3.29	2.08 1.49	2.74 2.17	0.67 0.65	0.43 0.43	2.03 2.20	1.55 1.53		4 3.5	4.62 3.62	3.85 2.97	1.99 1.52	1.11 0.81	0.83 0.82	0.24 0.22	1.93 1.96	1.63 1.62
	4.5	4.09	2.71	1.49	1.74		0.43	1.94	1.55		3.5	2.84	2.50	1.32		0.82	0.22	1.90	1.02
	3.5	3.14	2.07	0.95	1.35	0.66	0.43	2.17	1.45		2.5	2.14	1.70	0.88	0.59	0.79	0.28	1.93	1.68
	3 2.5	2.61 2.10	1.72 1.33	0.83 0.68	1.10 0.84	0.66 0.64	0.42 0.40	2.06 1.97	1.55 1.48		2 1.5	1.65 1.25	1.27 1.00	0.67 0.51	0.48 0.30		0.29 0.24	1.91 1.96	1.76 1.83
	2	1.72	1.14	0.57	0.67	0.66	0.39	1.99	1.53		1	0.92	0.80	0.44		0.87	0.18	1.82	1.97
	1.5 1	1.39 1.10	0.97 0.81	$0.48 \\ 0.46$	0.45 0.22	0.70 0.74	0.32 0.20	2.03 1.75	1.60 2.20		0.5 0	0.66 0.46	0.77 0.67	0.32 0.46		1.17		2.41	2.05
	0.5	0.74	0.81	0.40	0.22	1.04	0.20	1.75	2.20	C8276	5	7.55	6.20	3.40	1.47	0.82	0.19	1.82	1.59
C11440	0	0.47	0.70	0.47	e 77	0.70	0.26	1.00	1 50		4.5	5.98	5.07	2.68	1.14		0.19	1.89	1.59
C11440	6.5 6	15.97 12.68	11.23 8.91	5.66 4.53	5.77 4.73	0.70 0.70	0.36 0.37	1.98 1.97	1.58 1.56		4 3.5	4.74 3.72	4.06 3.25	2.16 1.72	0.86 0.65		0.18 0.18	1.88 1.89	1.63 1.70
	5.5	10.15	7.39	3.42	3.99	0.73	0.39	2.16	1.54		3	2.85	2.50	1.35	0.53	0.88	0.18	1.86	1.80
	5 4.5	8.17 6.61	5.59 4.60	2.73 2.13	3.30 2.71	0.68 0.70	0.40 0.41	2.04 2.16	1.53 1.51		2.5 2	2.13 1.61	1.82 1.32	0.98 0.74	0.41 0.33		0.19 0.20	1.85 1.79	1.75 1.82
	4	5.38	3.70	1.76	2.10	0.69	0.39	2.10	1.51		1.5	1.19	1.01	0.55	0.25	0.84	0.20	1.84	1.87
	3.5	4.37	2.93	1.52	1.68	0.67	0.39	1.93	1.59		1	0.87	0.78	0.39	0.15		0.18	1.98	2.05
	3 2.5	3.46 2.75	2.13 1.85	1.17 0.97	1.32 1.02	0.62 0.67	0.38 0.37	1.82 1.90	1.59 1.67		0.5 0	0.61 0.41	0.75 0.66	0.33 0.41		1.23		2.29	2.25
	2	2.13	1.36	0.75	0.78	0.64	0.36	1.80	1.73	C8423	6	11.18	8.59	4.44		0.77	0.25	1.93	1.52
	1.5 1	1.62 1.26	1.14 0.87	0.60 0.52	0.50 0.28	0.70 0.69	0.31 0.22	1.90 1.69	1.65 2.05		5.5 5	9.07 7.12	7.26 5.83	3.90 3.07	2.10 1.60		0.23 0.22	1.86 1.90	1.62 1.59
	0.5	0.88	0.86	0.47	0.20	0.97	0.22	1.83	2.91		4.5	5.65	4.69	2.45	1.20	0.83	0.21	1.91	1.58
C8272	0 7	0.52 17.65	0.72 12.86	0.52 7.44	4 10	0.73	0.23	1.73	1.52		4 3.5	4.49 3.52	3.90 3.06	1.99 1.68	0.81 0.55	0.87 0.87	0.18 0.16	1.96 1.82	1.62 1.69
C0272	6.5	14.29	10.60	6.10		0.73	0.23	1.73	1.52		3.5	2.71	2.38	1.08	0.33		0.10	1.82	1.73
	6	11.59	9.17	5.00	2.52	0.79	0.22	1.83	1.57		2.5	2.06	1.73	0.93	0.46		0.22	1.86	1.78
	5.5 5	9.26 7.40	7.27 6.10	4.07 3.24	1.95 1.47	0.79 0.82	0.21 0.20	1.79 1.88	1.57 1.60		2 1.5	1.54 1.12	1.23 0.94	0.67 0.50	0.37 0.27	$0.80 \\ 0.84$	0.24 0.24	1.83 1.89	1.89 1.87
	4.5	5.85	4.85	2.69	1.16	0.83	0.20	1.80	1.59		1	0.82	0.71	0.35	0.16	0.86	0.19	2.02	2.00
	4 3.5	4.64 3.63	3.93 3.18	2.01 1.63		$0.85 \\ 0.88$	0.22 0.21	1.96 1.95	1.64 1.67		0.5 0	0.58 0.40	0.71 0.65	0.31 0.40		1.21		2.25	2.06
	3	2.81	2.42	1.24	0.61	0.86	0.22	1.95	1.65		0	0.40	0.05	0.40					
	2.5	2.19	1.92	0.96	0.50		0.23	2.01	1.78										
	2 1.5	1.64 1.23	1.40 1.07	0.73 0.52	0.39 0.29	$0.85 \\ 0.87$	0.24 0.24	1.90 2.05	1.79 1.85										
	1	0.90	0.82	0.41		0.91	0.15	1.99	1.96	·	1 1			1					
	0.5 0	0.64 0.42	0.82 0.71	0.35 0.42		1.28		2.34	2.30	in this stu									
C9455	8	18.72	13.64	7.27		0.73	0.32	1.88	1.47	(number									
	7.5 7	15.46 12.92	11.34 9.82	5.42 4.91	5.13 4.17	0.73 0.76	0.33 0.32	2.09 2.00	1.43 1.48	wh: max width (c									
	6.5	12.92	9.82 8.44	3.85		0.70	0.32	2.00	1.46	expansio									
	6	8.83	7.00	3.32	2.85	0.79	0.32	2.11	1.46	$CWI_n = v$									
	5.5 5	7.31 6.04	5.97 5.05	2.67 2.42	2.22 1.56	0.82 0.84	0.30 0.26	2.24 2.08	1.47 1.51	whorl wi				a luul	muez	·, vv	•• • • <u>•</u> •	- •• •• n	, wm <sub>n</sub> ,
	4.5	4.92	4.11	2.06	1.15	0.84	0.23	2.00	1.55	WINDII WI	aur ma								
	4 3.5	3.95 3.19	3.33 2.75	1.71 1.31	0.93 0.72	0.84 0.86	0.23 0.22	1.95 2.09	1.54 1.52										
	3.5 3	2.58	2.75	1.16		0.80		1.87	1.52	Accepted: 3	3 April 20	20							